

MCA (Revised)
Term-End Examination
June, 2009

MCS-013 : DISCRETE MATHEMATICS

Time : 2 hours

Maximum Marks : 50

Note : Question number 1 is compulsory. Attempt any three questions from the rest.

1. (a) A coin is tossed n times. What is the probability of getting exactly r heads ? 3
- (b) Construct the logic circuit for the expression $(x_1' \wedge x_2) \vee (x_1 \vee x_3)$ 3
- (c) Let the function $f : \mathbb{R} \rightarrow \mathbb{R}$ be defined by 3

$$f(x) = \begin{cases} 3x-12 & \text{for } x > 3 \\ 2x^2+3 & \text{for } -2 < x \leq 3 \\ 3x^2-7 & \text{for } x \leq -2 \end{cases}$$

Find out $f^{-1}(5)$.

- (d) Universal Set $U = \{1, 2, \dots, 9\}$ and given 4
the sets $A = \{1, 2, 3, 4, 5\}$,
 $B = \{4, 5, 6, 7\}$.

- Find (i) $A \setminus B$
(ii) $A \oplus B$

- (e) Consider a set $A = \{a, b, c\}$ and the relation R on A defined by $R = \{ (a, a), (a, b), (b, c), (a, c) \}$. Find whether R is : 3

- (i) reflexive
- (ii) symmetric
- (iii) transitive

Justify your answers with reason.

- (f) A survey among 1000 people, 595 are democrats, 595 wear glasses and 550 like ice-creams. 395 of them are democrats who wear glasses, 350 of them are democrats who like ice-cream. 400 of them wear glasses and like ice cream and 250 have all the three properties. 4

- (i) How many of them are not democrats do not wear glasses and do not like ice creams ?
- (ii) How many of them are democrats who do not wear glasses and do not like ice cream ?

2. (a) Show that $(P \wedge (P \rightarrow q)) \rightarrow q$ is tautology. 3
- (b) Find DNF form of $7(PVQ) \leftrightarrow PAQ$ 4
- (c) Prove that for every positive integer n , $n^3 + n$ is even. 3

3. (a) By the principal of mathematical induction, prove that : 4
 $3^{2n+1} + (-1)^n 2$ is divisible by 5.
- (b) Define the De-Morgan's Laws for complementation. Further illustrate with suitable examples. 3
- (c) Find the coefficient of x^2y^4 in $(x+y)^6$. 3
4. (a) Write down all the partitions of 7. Also find P_7^4 and P_7^5 . 4
- (b) By contrapositive method of proof, prove that x^2 is divisible by 4, then x is even. 3
- (c) Establish the equivalence 3
 $(P \rightarrow Q) \rightarrow (P \wedge Q) \equiv (7P \rightarrow Q) \wedge (Q \rightarrow P)$
5. (a) If set X has 10 members, how many members do $P(X)$ has ? How many members of $P(X)$ are proper subset of X ? 3
- (b) Prove that $A - (A - B) = A \cap B$ 3
- (c) Let $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = ax + b$ 4
 where $a, b, x \in \mathbb{R}$, and $a \neq 0$. Show that f is invertible and find the inverse of f .

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